## Homework 5

Posted: November 25, 2024 Due: December 11, 2024

- 1. Show that the function f(u, v) = uv is computable in  $\mathcal{S}_n$ . Recall that uv denotes the concatenation of the words u and v.
- 2. Let  $A = \{s_1, \ldots, s_n\}$  and let P(x) be the predicate on  $A^*$  that is TRUE just when x has an even number of symbols. Show that P(x) is computable in  $S_n$ .
- 3. Define  $\operatorname{HALT}_n(x, y)$  as the predicate that is TRUE if and only if the  $\mathcal{S}_n$  program y eventually halts on input x. Show that  $\operatorname{HALT}_n(x, y)$  is not computable in  $\mathcal{S}_n$ .
- 4. Construct a Post-Turing program that computes strictly the function f(u, v) = uv.
- 5. Construct a Turing machine that computes the function  $f(x) = x^R$ .