Storage En	igine vs. QP (Query Processor)				
	User \$QL Query				
	Query Compiler				
Query Processor	Query Plan (optimized)				
Query 110000000	Execution Engine				
Storage engine AF	Index and Record requests				
Storage engine	Index/File/Record Manager				
	Page Commands				
Buffer Manager					
	Read/Write pages				
	Disk Space Manager				
	Disk I/O				
	Data				
A first course in database sys	stems, 3 rd ed, Ullman and Widom				

I/O Cost Model, Tree Indexes

CS634 Lecture 5, Feb 10, 2016

Slides based on "Database Management Systems" 3rd ed, Ramakrishnan and Gehrke

Cost Model and Performance Analysis

Focus on I/O cost (bulk of the processing cost)

- **B** The number of data pages in file
- **R** Number of records per page
- D Average time to read or write disk page
- F Fanout of tree index

Operations to compare:

- Scan
- Equality search
- Range selection
- Insert a record
- Delete a record

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Storage Engine API

- Example: The mysql storage engine API has calls to "ha_open" a table, "ha_init_index" to specify the index to use if any, "index_read" to fetch a row by key using the current table and the current index.
- In general, the storage engine can work with one file of records, or two files, one of "data records" and one that is some kind of index for the first file. It can't process more files at once. Two index files are also possible, though not covered in this chapter.
- It's the job of the QP to break down the needed work into the small steps that the storage engine can do.

▶ 4

Compared File Organizations

- Heap file
- Sorted file
- Clustered B+ tree file
- AKA clustered file
- Heap file with unclustered B+ tree index (2 files involved)
- Heap file with unclustered hash index (2 files involved)

Cost Model: Heap Files (unsorted)

Given:

- B The number of data pages in file
- R Number of records per page
- > D Average time to read or write disk page
- Scan B data pages, each takes read time D
- So i/o Cost = B*D
- Equality Search, for unique key: i/o Cost = 0.5*B*D
- Range Search: B*D
- Insert: read, write last page: 2*D
- > Delete, given key: equality search, then rewrite page
- Delete, given RID: 2*D
- We never used R!
- > One problem: D depends on how much seeking is needed

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Size of D, time for one page access

- If pages are laid out sequentially on a track, the disk can pull them off in one rotation. D may be .1 ms. or less.
- If pages are randomly situated on the disk, the seek time dominates pages smaller than IMB in size. D is about 3-5 ms.
- A Common page size is 8KB.
- For this chapter, we paste over the difference and pretend D is constant, say 1 ms. for easy calculation.

Tree-Index Assumptions

Tree Indexes:

- Alternative (1) data entry size = size of record
- Alternative (2): data entry size = 10% size of record
- 67% occupancy (this is typical) Note 1/.67 = 1.5
 File size = 1.5 data size
- Scans:
 - Leaf levels of a tree-index are chained.
- Index data-entries plus actual file scanned for unclustered indexes (unrealistic, will revisit)
- Range searches:
 - We use tree indexes to restrict the set of data records fetched, but ignore hash indexes for now

▶ 8

Basic Analysis for Tree Indexes

- B = # pages to hold row data compactly ("data size")
- Alternative (1) data entry size = size of record
- Alternative (2) data entry size = 10% size of record
 This is an assumption for simplicity of analysis.
- 67% occupancy, Note 1/.67 = 1.5, so 50% expansion on disk to allow 33% space on pages for new rows.
 - (Actually, follows from B-Tree algorithms)
 - File size = 1.5 data size,

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▶ 11

- Alternative (1): NLeafPgs = 1.5*B
- Alt. (2): NDataPgs = 1.5*B, NLeafPgs = .10*1.5*B = .15*B



Pages (Sorted by search key) NLeafPgs ~ F^h

So tree height $h \sim \log_F(NLeafPgs) = \log_F(1.5*B)$, alt (1) $h \sim \log_F(NLeafPgs) = \log_F(.15*B)$, alt (2)

Search down tree takes time = h*D, assuming nothing in buffer

▶ 10

CLUSTERED Data entries (ndex File)

Clustered vs. Unclustered Index

- To build clustered index, first sort the heap file, leaving some free space on each page for future inserts
- Overflow pages may be needed for inserts
 Hence order of data records is close to the sort order

Cost of Operations (Page 291) B=#data pgs, R=#recs/pg, D=disk time, F=fanout

	(a) Scan	(b) Equality	(c) Range	(d) Insert	(e) Delete
(1) Heap	BD	0.5BD	BD	2D	Search +D
(2) Sorted	BD	Dlog 2B	D(log 2 B + # pgs with match recs)	Search + BD	Search +BD
(3) Clustered	1.5BD	Dlog F 1.5B	D(log F 1.5B + # pgs w. match recs)	Search + D	Search +D
(4) Unclust. Tree index	BD(R+0.15)	D(1 + log F 0.15B)	D(log F 0.15B + # pgs w. match recs)	Search + 2D	Search + 2D
(5) Unclust. Hash index	BD(R+0.125)	2D	BD	Search + 2D	Search + 2D

Scan of Unclustered tree index

➢ Fig. 8.4 says i/o cost = BD(R+0.15) ▶ But this means actively using the index and chasing each data entry into the heap. >No serious database does this. >Instead, the database scans the underlying heap, at cost BD. Similarly for the unclustered hash index

Tree Indexes

- Tree-structured indexing techniques support efficiently range searches
- equality searches

► ISAM

- Indexed Sequential Access Method, developed by IBM long ago Static tree structure
- ISAM has another meaning: An API allowing indexed lookup by key and next-ing through successive rows/records after the first lookup.

▶ B+ tree:

- Dynamic structure
- Adjusts gracefully under inserts and deletes

Tree Indexes Intuition

How to answer efficiently range query on k?

- Option: store data in sorted file on \mathbf{k} and do binary search Þ
- Þ Find first matching record, then scan to find others
- But cost of binary search is high (not to mention inserts)
- Simple idea: Create an index file
- First key value in each data page placed in an index page



ISAM

Index file may still be quite large

> Apply the idea repeatedly on previous index level!



Building an ISAM

First, create leaf level (data entries)

- Allocate index leaf pages sequential on disk
- Alternative I natural choice for ISAM (data records inside data entries) - this way data are also sequential on disk
- Sequential allocation increases performance of range queries

Next, create internal (index) nodes

- These will never change after initialization
- Index entries: <search key value, page id>
- b direct search for data entries, which are in leaf pages
- Finally, allocate overflow pages
 - If needed, when insertions are performed

ISAM Operations

Search

- > Start at root, use keys to guide search towards leaf nodes Cost is log F N
- F = # entries/index node page, N = # leaf pages in tree
- Insert
 - Find leaf data entry where records belongs
 - If no space, create an overflow page
- Delete
 - > Find and remove from leaf
- If empty overflow page, de-allocate

Static tree structure: inserts/deletes affect only leaf pages!

Does not require locking the internal nodes!

But not available as an access method in any DB, even DB2.

Example ISAM Tree



After Inserting 23*, 48*, 41*, 42*



Then Deleting 42*, 51*, 97*



Note that 51* appears in index levels, but not in leaf!

- B+ Tree
- MostWidely Used Index
- Dynamic data structure (as opposed to ISAM)
- Tree is height-balanced
 - Height is log F N (F = fanout, N = # leaf pages)
 - But fanout isn't really a constant...
- Minimum 50% occupancy constraint
 - Each node (except root) contains d <= m <= 2d entries</p>
 - Parameter **d** is called the order of the tree (min fanout)
- Search just like in ISAM
 - But insert/delete more complex due to occupancy constraint
- Insert/delete may trigger re-structuring at all levels of tree

B+ Tree Example

> Search begins at root, key comparisons direct it to a leaf



Based on the search for 15*, we know it is not in the tree!

B+ Trees in Practice

- Recall rule d <= m <= 2d,</p>
- Here d = order, m = # entries/page = fanout
- Typical order: 100 (min fanout) So max fanout = 2*100 = 200, for full page
- Typical fill-factor:67%
- Results on average fanout F = .67*200 = 133
- Typical capacities:
 - Height 4: 133⁴ = 312,900,700 leaf pages Height 3: 133³ = 2,352,637 leaf pages
- Each leaf page corresponds to .67 page of row data (alt (1)) or 6.7 pages of row data (alt(2) using 10% size assumption)
- Can often hold top levels in buffer pool: assuming 8KB pages: 8 KB
 - Level I = l page
 - 133 pages Level 2 = = Level 3 = 17,689 pages
- = 133 MB Level 4 = 2,352,637 pages = 18 GB (probably not in pool)

I MB

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B+ Tree Example: Insert 8* (d=2)



Example B+ Tree After Inserting 8*



Root was split, leading to increase in height

We can avoid split by re-distributing entries, but this is usually not done in practice for insertions

B+ Tree Insertion Algorithm

- Find correct leaf L
- Place data entry in L
 - If L has enough space, done!
 - Else, must **split** *L* (into *L* and a new node *L*2) Redistribute entries evenly, <u>copy up</u> middle key
- Insert index entry pointing to L2 into parent of L This can happen recursively
 - To split index node, redistribute entries evenly, but push up middle key
- > Splits "grow" tree; root split increases height.
 - Tree growth: gets wider or one level taller at top



Then Delete 24*

- Must merge with sibling
- Index entry 27 is deleted, due to removal of leaf node



pull down of index key from parent



Non-leaf Re-distribution



B+ Tree Deletion Algorithm

- Start at root, find leaf L where entry belongs
- Remove the entry
 - If L is at least half-full, done!
 - If L has only d-I entries
 - Try to re-distribute, borrowing from sibling
 - If re-distribution fails, merge L and sibling
- If merge occurred, must delete entry from parent of L
- Merge could propagate to root, decreasing height

Bulk Loading of a B+ Tree (d=1)

- Method to efficiently build a tree for first time
 - Much better than doing repeated insertions
 - Can place pages sequentially on disk
- Sort all data entries, insert pointer to first leaf page in a new root page



Bulk Loading (Contd.)

Index entries for leaf pages always entered into right-most index page just above leaf level



10 11 12 13

20'22" 23'31"

10 20

B+ Tree: Prefix Key Compression

- Good I/O performance due to low tree height
- Important to increase fan-out
- Key values in index entries only direct search
- Sometimes keys can be long (e.g., long names)
- It is possible to compress them
- Key Compression Rule
- > Each index entry greater than every key value (in any subtree) to its left
- Insert/delete must be suitably modified

Summary

- Tree-structured indexes are ideal for range-searches, also good for equality searches.
- ISAM tree is a static structure.
 - Only leaf pages modified; overflow pages needed.
 - Overflow chains can degrade performance unless size of data set and data distribution stay constant.
- B+ tree is a dynamic structure.
 - Inserts/deletes leave tree height-balanced; log F N cost.
 - High fanout (F) means depth rarely more than 3 or 4.
 - Almost always better than maintaining a sorted file.

Summary (Contd.)

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- Typically, 67% occupancy on average.
- Usually preferable to ISAM; adjusts to growth gracefully.
- But concurrency control (locking) is easier in ISAM
- > If data entries are data records, splits can change rids!
- Key compression increases fanout, reduces height.
- Bulk loading can be much faster than repeated inserts for creating a B+ tree on a large data set.
- Most widely used index in database management systems because of its versatility. One of the most optimized components of a DBMS.