Data Structures and Algorithms in Java

Assignment 2 (Global Sequence Alignment) Discussion

Part I (Warmup Problems) · Problem 1 (Reverse)

C	🕼 Reverse. java						
	Standard input	a sequence of strings					
	Standard output	the strings in reverse order					

2_ ~/workspace/global.sequence.alignment	
β javac −d out src/Reverse.java \$ java Reverse	
bolton <ctrl-d></ctrl-d>	
a o t 1 o b \$ java Reverse	
n a d' a m <ctrl-d></ctrl-d>	
hadam	

Read all strings from standard input into an array *a* (use stdIn.readAllStrings())

Set n to the size of a

For each int $i \in [0, n/2)$

- Exchange a[i] with a[n - i - 1]

For each int $i \in [0, n)$

- If i < n - 1, write a[i] with a space after; otherwise, write a[i] with a newline after

Part I (Warmup Problems) · Problem 2 (Euclidean Distance)

istance.java				
Command-line input	n (int)			
Standard input	two size- n arrays x and y of doubles			
Standard output	the Euclidean distance between the two vectors represented by x and y			

>_ ~/w	orkspace/global.sequence.alignment
\$ jav	vac -d out src/Distance.java
\$ jav	va Distance 2
) 1 <enter></enter>
1.414	12135623730951
\$ jav	va Distance 5
	10 -1 1 -5 9 6 7 4 <enter></enter>

Part I (Warmup Problems) · Problem 2 (Euclidean Distance)

Accept n (int) as command-line argument

Create a size-n array x of doubles

For each int $i \in [0, n)$

- Set a[i] to a double read from standard input (use stdIn.readDouble())

Create and initialize a size-n array y of doubles similar to x

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Set sum (double) to 0
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For each int $i \in [0, n)$

- Increment sum by $(x[i] - y[i])^2$

Write \sqrt{sum}

Part I (Warmup Problems) · Problem 3 (Transpose)

🕼 Transpose.java					
Command-line input	<i>m</i> (int) and <i>n</i> (int)				
Standard input	m imes n doubles representing the elements of an $m imes n$ matrix a				
Standard output	the transpose of a				

_ ~/workspace/global.sequence.alignment	
javac -d out src/Transpose.java	
java Transpose 2 2	
2 3 4 <enter></enter>	
; java Transpose 2 3	
2 3 4 5 6 <enter></enter>	
3.0 6.0	

Part I (Warmup Problems) · Problem 3 (Transpose)

Accept m (int) and n (int) as command-line arguments

Create an $m \times n$ array *a* of doubles

For each int $i \in [0, m)$

- For each int $j \in [0, n)$
 - Set a[i][j] to a double read from standard input (use stdIn.readDouble())

Create an $n \times m$ array c of doubles

```
For each int i \in [0, n)
```

```
- For each int j \in [0, m)
```

Set c[i][j] to a[j][i]

```
For each int i \in [0, n)
```

- For each int $j \in [0, m)$

- If j < m - 1, write c[i][j] with a space after; otherwise, write c[i][j] with a newline after

Part I (Warmup Problems) · Problem 4 (Strange Matrix)

C	🕼 StrangeMatrix.java						
	Command-line input	m (int) and n (int)					
	Standard output	an $m imes n$ (strange) matrix					

>_	_ ~/workspace/global.sequence.alignment												
69 69	javac java S 147 54	-d out Strange 66 27	src/S Matrix 27 12	Strange : 4 5 10 5	eMatrix. 3 2	. java							

Part I (Warmup Problems) · Problem 4 (Strange Matrix)

Accept m (int) and n (int) as command-line arguments

Create an $m \times n$ array *a* of ints

```
For each int i \in [0, m)

- Set a[i][n - 1] to m - i - 1

For each int j \in [0, n)

- Set a[m - 1][j] to n - j - 1

For each int i \in [m - 2, 0]

- For each int j \in [n - 2, 0]

- Set a[i][j] to a[i][j + 1] + a[i + 1][j + 1] + a[i + 1][j]
```

For each int $i \in [0, m)$

- For each int $j \in [0, n)$

- If j < n-1, write a[i][j] with the format string "X5d "; otherwise, write a[i][j] with the format string "X5d\n"

Part I (Warmup Problems) · Problem 5 (Pascal's Triangle)

C	🕼 Pascal.java						
	Command-line input	n (int)					
	Standard output	Pascal's triangle \mathcal{P}_n					

>_ ~	/workspace/global_sequence_alignment
\$ j	avac -d out src/Pascal.java
\$ j	ava Pascal 5
1 2	
1 3	
1 4	
15	

Part I (Warmup Problems) · Problem 5 (Pascal's Triangle)

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Accept n (int) as command-line argument
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Create a 2D array a of ints with n + 1 rows (leave the column capacity empty)

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For each int i \in [0, n]

- Set a[i] to an array of i + 1 ints

- For each int j \in [0, i]

- Set a[i][j] to 1

For each int i \in [0, n]

- For each int j \in [1, i)

- Set a[i][j] to a[i - 1][j - 1] + a[i - 1][j]
```

```
For each int i \in [0, n]
```

- For each int $j \in [0, i]$
 - If j < i, write a[i][j] with a space after; otherwise, write a[i][j] with a newline after

Part II (Global Sequence Alignment) · Introduction

Goal: find an optimal alignment for two DNA sequences ${\tt x}$ and ${\tt y}$

We are permitted to insert gaps in either sequence to make them have the same length

We pay a penalty for each gap that we insert and also for each pair of characters that mismatch

Operation	Cost
Insert a gap	2
Align two characters that do not match	1
Align two characters that do match	0

Part II (Global Sequence Alignment) · Introduction

Edit distance is the cost of the best possible alignment between the two genetic sequences over all possible alignments

Two possible alignments of the sequences x = "AACAGTTACC" and y = "TAAGGTCA"

	cost		

Edit distance for the two sequences is 7

Part II (Global Sequence Alignment) · Notation

m and n denote the lengths of x and y, respectively

 ${\tt x[i]}$ denotes the ith character of the sequence ${\tt x}$

x[i..m] denotes the suffix of x consisting of the characters x[i], x[i + 1], ..., x[m - 1]

opt is the (m + 1) x (n + 1) edit-distance matrix

 $_{\tt opt[i][j]}$ denotes the edit distance of $_{\tt x[i..m]}$ and $_{\tt y[j..n]}$

Example: if x = "AACAGTTACC" and y = "TAAGGTCA", then

- m = 10 and n = 8
- x[2] is 'C'
- $_{\rm x[5..m]}$ is "Cagttacc" and $_{\rm y[8..n]}$ is ""
- opt is a 11 x 9 matrix
- $_{opt}$ [0] [0] is the edit distance of x and y

Part II (Global Sequence Alignment) · Recursive Solution

Case 1 (x[i] is matched with y[j]): opt[i][j] = opt[i + 1][j + 1] + 0 or 1 depending on whether x[i] equals y[j]

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Case 2 (x[i] is matched with a gap): opt[i][j] = opt[i + 1][j] + 2
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Case 3 (y[j] is matched with a gap): opt[i][j] = opt[i][j + 1] + 2
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We compute <code>opt[i][j]</code> by taking the minimum of the three quantities

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opt[i][j] = min(opt[i + 1][j + 1] + 0 or 1, opt[i + 1][j] + 2, opt[i][j + 1] + 2)
```

Direct computation of this recursive scheme is spectacularly inefficient

We use dynamic programming

Key idea: break up a large problem into smaller subproblems, store the answers to those smaller subproblems, and use the stored answers to solve the original problem

Part II (Global Sequence Alignment) · Problem 6 (Compute Edit Distance)

Write a program called EditDistance.java that reads strings x and y from standard input; computes the edit-distance matrix opt; and outputs x, y, the dimensions of opt, and opt

>_ "/workspace/global_sequence_alignment											
\$ ja \$ ja AACA TAAG 11 9	<pre>\$ javac -d out src/EditDistance.java \$ java EditDistance < data/example10.txt AACACTTACC TAAGGTCA 11 9</pre>										
							14				

Read sequences x (String) and y (String) from standard input

Set m (int) and n (int) to the lenghts of x and y, respectively (use GSA.length(y))

Create an $(m + 1) \times (n + 1)$ array opt of ints

Initialize the rightmost column of opt to 2(m - i), where $0 \le i \le m$

Initialize the bottommost row of opt to 2(n - j), where $0 \le j \le n$

Part II (Global Sequence Alignment) · Problem 6 (Compute Edit Distance)

Fill in the rest of opt, starting at opt[m - 1] [m - 1] and ending at opt[0][0], as follows (use GSA.charAt() and GSA.min() where needed)

- $\ \ If \ x[i] = y[j] \ then \ opt[i][j] = min(opt[i + 1][j + 1], \ opt[i + 1][j] + 2, \ opt[i][j + 1] + 2)$
- Otherwise, opt[i][j] = min(opt[i + 1][j + 1] + 1, opt[i + 1][j] + 2, opt[i][j + 1] + 2)

Write the following output, each starting on a new line

- x

- у

- m and n separated by a space
- opt using the format string "X3d " for elements not in the last column, and "X3d\n" for the last-column elements

Part II (Global Sequence Alignment) · Problem 7 (Recover Alignment)

Write a program Alignment.java that reads from standard input the output produced by EditDistance.java; recovers an optimal alignment between x and y; and writes the edit distance and the alignment

>_ ~/vorkspace/global.sequence.alignment	
<pre>\$ javac -d out src/Alignment.java \$ java EditDistance < data/example10.txt java Alignment 7 A T 1 A A 0 C - 2 A A 0 C G 0 C G 0 T G 1 T T 0 A - 2 C C 0 C A 1</pre>	

Read sequences x (String) and y (String) from standard input

Set m (int) and n (int) to the lenghts of x and y, respectively

Read the edit-distance matrix opt from standard input (use stdArrayI0.readInt2D())

Write the edit distance between x and y, ie, the value of opt[0][0]

Set ints \mathtt{i} and \mathtt{j} both to \mathtt{o}

Recover and output the optimal alginment, starting at $_{opt [0][0]}$ and ending at $_{opt [m - 1][m - 1]}$, as follows

- If opt[i][j] = opt[i + 1][j] + 2, then align x[i] with a gap and penalty of 2, and increment i
- Otherwise, if opt[i][j] = opt[i][j + 1] + 2, then align y[j] with a gap and penalty of 2, and increment j
- Otherwise, align x_{13} with y_{13} with a penalty of 0 or 1 depending on whether x_{13} equals y_{13} , and increment both a and y_{13}

If y is exhausted before x (ie, i < m), align the remaining x with gaps and penalty of 2

If x is exhausted before y (ie, j < n), align the remaining y with gaps and penalty of 2