

UMass Boston Computer Science  
**CS450 High Level Languages** (section 2)

# **Interpreting Recursion, with Mutation!**

Monday, December 2, 2024

## *Logistics*

- HW 12 out
  - due: Sun 12/4 12pm (noon) EST

# “bind” in “CS450” Lang

```
;; A Variable (Var) is a Symbol
```

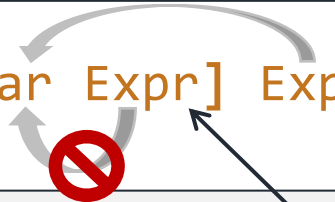
```
;; A 450LangExpr (Expr) is one of:  
;; ...  
;; - Var  
;; - '(bind [Var Expr] Expr)  
;; ...
```

Reference a variable binding

new binding is in-scope  
(can be referenced) here

Create new  
variable binding

new binding is not  
in-scope here



# bind examples

```
;; A 450LangExpr (Expr) is one of:  
;; ...  
;; - Var  
;; - '(bind [Var Expr] Expr)  
;; ...
```

```
(check-equal?  
  (eval450  
    '(bind [x (+ x 20)]  
           x))  
  UNDEFINED-ERROR )
```

???

# bind examples, with functions

```
;; A 450LangExpr (Expr) is one of:  
;; ...  
;; - Var  
;; - '(bind [Var Expr] Expr)  
;; - '(fn List<Var> Expr)  
;;   (cons Expr List<Expr>)  
;; ...
```

"lambda"  
function

function

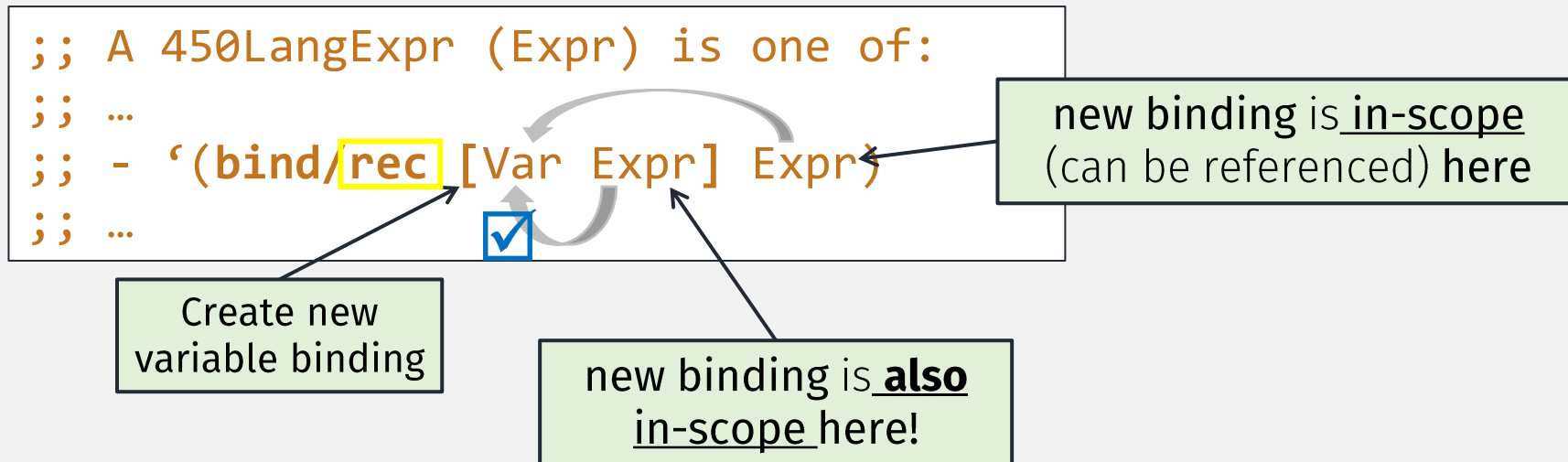
arguments

function call

```
(check-equal?  
  (eval450  
    '(bind [f (fn (x) (+ x 4))]  
           (f 6)))  
  10 )
```

f not in-scope here  
(so function can't be recursive!)

# “bind/rec” in “CS450” Lang



# Racket recursive function examples

```
(define (fac n)
  (if (= n 0)
      1
      (* n (fac (- n 1)))))
```

(fac 5) ; => 120

RACKET

Equivalent to ...

```
(letrec
  ([fac
   (lambda (n)
     (if (= n 0)
         1
         (* n (fac (- n 1)))))])
  (fac 5)) ; => 120
```

RACKET

# bind/rec examples

```
;; A 450LangExpr (Expr) is one of:  
;; ...  
;; - '(bind/rec [Var Expr] Expr)  
;; - '(Expr ? Expr : Expr)  
;; ...
```

JS “truthy if” (hw10)

```
(letrec  
  ([fac  
    (λ (n)  
      (if (= n 0)  
          1  
          (* n (fac (- n 1))))))]  
  (fac 5)) ; => 120
```

RACKET

Equivalent to ...

```
(bind/rec  
  [fac  
    (fn (n)  
      (n ? (* n (fac (- n 1)))  
           : 1))]  
  (fac 5)) ; => 120
```

CS450LANG

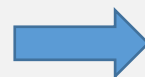
Zero is “truthy” false (hw10)



# Running `bind/rec` programs

```
;; A 450LangExpr (Expr) is one of:  
;; ...  
;; - '(bind/rec [Var Expr] Expr)  
;; ...
```

parse



```
;; An AST is one of:  
;; ...  
;; - (recb Symbol AST AST)  
;; ...  
(struct recb [var expr body])
```

run



```
;; A Result is a:  
;; - ...
```

# Running `bind/rec` programs

TEMPLATE ?

```
;; run: AST -> Result  
;; Computes result of  
running CS450 Lang AST
```

```
;; An AST is one of:  
;; ...  
;; - (recb Symbol AST AST)  
;; ...  
(struct recb [var expr body])
```

run



```
;; A Result is a:  
;; - ...
```

# Running `bind/rec`

TEMPLATE : extract pieces

```
;; run: AST -> Result
```

```
(define (run p)
```

```
  (define (run/e p env)
```

```
    (match p
```

```
      ...
```

```
      [(recb x e body) ?? x ?? e ?? body ]))
```

```
      ... ))
```

```
(run/e p ??? )
```

```
;; An AST is one of:
```

```
;; ...
```

```
;; - (recb Symbol AST AST)
```

```
;; ...
```

```
(struct recb [var expr body])
```

# Running `bind/rec`

TEMPLATE : recursive call

```
;; run: AST -> Result
```

```
(define (run p)
```

```
  (define (run/e p env)
```

```
    (match p
```

```
      ...
```

```
      [(recb x e body) ?? x ?? (run/e e ??) ?? (run/e body ??) ]])
```

```
      ... ))
```

```
(run/e p ??? )
```

```
;; An AST is one of:
```

```
;; ...
```

```
;; - (recb Symbol AST AST)
```

```
;; ...
```

```
(struct recb [var expr body])
```

# Running `bind/rec`, using environment

```
;; run: AST -> Result
```

```
;; An Environment (Env) is one of:  
;; - empty  
;; - (cons (list Var Result) Env)
```

```
(define (run p)
```

```
  ;; accumulator env : Environment
```

```
  (define (run/e p env)
```

```
    (match p
```

```
      ...
```

```
      [(recb x e body) ?? x ?? (run/e e ??) ?? (run/e body ??) ]
```

```
      ... ))
```

```
  (run/e p INIT-ENV ))
```

# Running `bind/rec`, using environment

```
;; run: AST -> Result
```

```
(define (run p)
  ;; accumulator env : Environment
  (define (run/e p env)
    (match p
      ...
      [(recb x e body)
       (define env/x (env-add env x (run/e e env)))
       (run/e body env/x)]
      ... ))
  (run/e p INIT-ENV ))
```

2. add x binding to environment

1. Compute Result for x

# Running `bind/rec`, using environment

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```
;; run: AST -> Result
```

```
(define (run p)
  ;; accumulator env : Environment
  (define (run/e p env)
    (match p
      ...
      [(recb x e body)
       (define env/x (env-add env x (run/e e env/x)
                              (run/e body env/x))]
       ... ))
    (run/e p INIT-ENV
```

Compute body  
with x in-scope

```
(bind/rec
 [fac ←
  (fn (n)
    (n ? (* n (fac (- n 1)))
      : 1))]
 (fac 5)) ; => 120
```

??? This is circular! (no base case)

PROBLEM:  
x should be in-scope here too!

## *Interlude:* Mutation

- **Mutating** a variable means: to change its value after it is defined

```
(define x 3)
(display x) ; 3
(set! x 5) ; mutate x
(display x) ; 5
```



## *Interlude:* Mutation

- **Mutating** a variable means to change its value after it is defined
- **Mutation** should be rarely used, only in appropriate situations

# Interlude: Mutation

- Mutating a variable means to change its value after it is defined
- **Mutation** should be rarely used, only in appropriate situations

*Item 3: Use const whenever possible.*  
*Effective C++, Scott Meyers, 2005.*

Item 15, "Minimize mutability." **Joshua Bloch** Author, *Effective Java, Second Edition*

Joshua Bloch, Google's chief Java architect, is a former Distinguished Engineer at Sun Microsystems, where he led the design and implementation of numerous Java platform features, including JDK 5.0 language enhancements and the award-winning Java Collections Framework.

Immutability  
makes code  
easier to read  
and understand

Item 15 tells you to keep the state space of each object as simple as possible. If an object is immutable, it can be in only one state, and you win big. You never have to worry about what state the object is in, and you can share it freely, with no need for synchronization. If you can't make an object immutable, at least minimize the amount of mutation that is possible. This makes it easier to use the object correctly.

# Interlude: Mutation

- **Mutating** a variable means to change its value after it is defined
- **Mutation** should be rarely used, only in appropriate situations

Because:

- It makes code more difficult to read
  - (just like inheritance and dynamic scope)
- It violates “Separation of concerns”

```
(define x 3)
(do-something x) ; mutate x??
(display x) ; ???
```

# *Interlude:* Mutation

- **Mutating** a variable means to change its value after it is defined
- **Mutation** should be rarely used

When is using **mutation** ok:

- **Performance**
  - Typically **not using high-level languages!** (OS, AAA game i.e., not this class!)
  - Beware of **pre-mature optimization!**
- **Shared state** (in distributed programs)
  - Beware of **race conditions and deadlock!**
- **Circular data structures** (e.g., circular lists)

# Running `bind/rec`, recursive environment items

```
;; run: AST -> Result
```

```
(define (run p)
  (define (run/e p env)
    (match p
      ...
      [(recb x e body)
       (define env/x (env-add env x (run/e e env/x)))
       (run/env body env/x)]
      ...
      ))
  (run/e p INIT-ENV ))
```

??? This is **circular!** (no base case)

PROBLEM:  
x should be in-scope here too!

Compute body  
with x in-scope

# Running `bind/rec`, recursive environment items

```
;; run: AST -> Result
```

```
(define (run p)
  (define (run/e p env)
    (match p
      ...
      [(recb x e body)
       (define placeholder (box CIRCULAR-ERROR))
       (define env/x (env-add env x placeholder))

       (run/env body env/x)]
      ... ))
  (run/e p INIT-ENV))
```

Creates mutable box  
Makes mutation explicit

```
;; A Result is a:
;; - Number
;; - FunctionResult
;; - ErrorResult
```

```
;; An ErrorResult is a:
;; - UNDEFINED-ERROR
;; - ARITY-ERROR
;; - CIRCULAR-ERROR
```



# Running `bind/rec`, recursive environment items

```
;; run: AST -> Result
```

```
(define (run p)
  (define (run/e p env)
    (match p
      ...
      [(recb x e body)
       (define placeholder (box CIRCULAR-ERROR))
       (define env/x (env-add env x placeholder))

       (run/env body env/x)]
      ... ))
  (run/e p INIT-ENV ))
```

```
;; An Environment (OLD) (Env) is one of:
;; - empty
;; - (cons (list Var Result) Env)
```

???

(how would env-add and env-lookup need to change?)

```
;; An Environment (Env) is a: List<EnvVal>
```

```
;; An EnvVal is one of:
;; - Result
;; - Box<Result>
```

env/x



# Running `bind/rec`, recursive environment items

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```
(bind/rec [f f] f)  
; => CIRCULAR-ERROR
```

```
;; run: AST -> Result
```

```
(define (run p)  
  (define (run/e p env)  
    (match p ...  
      [(recb x e body)  
       (define placeholder (box CIRCULAR-ERROR))  
       (define env/x (env-add env x placeholder))  
       (define x-result (run/env e env/x))  
       (run/env body env/x)]  
      ... ))  
  (run/e p INIT-ENV))
```

Compute `x`'s  
Result with  
`x` in-scope!

Non-function, circular recursive  
references (no base case)  
produce error results!

env/x

...	...
x	CIRCULAR-ERROR



# Running `bind/rec`, recursive environment items

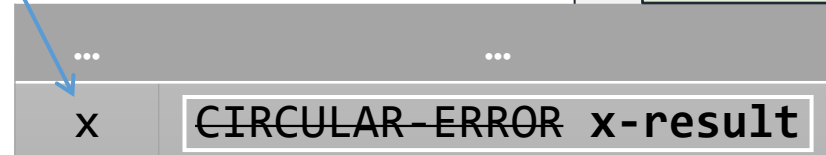
```
;; run: AST -> Result
```

```
(define (run p)
  (define (run/e p env)
    (match p
      ...
      [(recb x e body)
       (define placeholder (box CIRCULAR-ERROR))
       (define env/x (env-add env x placeholder))
       (define x-result (run/env e env/x))
       (set-box! placeholder x-result)
       (run/env body env/x)]
      ... ))
  (run/e p INIT-ENV ))
```

Close the (circular data structure) loop, with **mutation!**

Explicitly mutate mutable box

env/x



# Running `bind/rec`, recursive environment items

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```
;; run: AST -> Result
```

```
(define (run p)
  (define (run/e p env)
    (match p
      ...
      [(recb x e body)
       (define placeholder (box CIRCULAR-ERROR))
       (define env/x (env-add env x placeholder))
       (define x-result (run/env e env/x))
       (set-box! placeholder x-result)
       (run/env body env/x)]
      ...
      ))
  (run/e p INIT-ENV ))
```

Compute body  
with `x` in-scope

```
(bind/rec
 [fac
  (fn (n)
    (n ? (* n (fac (- n 1)))
      : 1))]
 (fac 5)) ; => 120
```



env/x



# HW 13 Preview: Recursion!

Use “CS450 LANG”! ... to write recursive programs:

- `fac` (factorial)
- `filt` (filter)
- `qsort` (functional quicksort)
- `gcd`
- `sierpinski` (fractal)

(Extra primitives will be added to `INIT-ENV`, ask if you need more)

- Look it up if you don't know any of these
  - Using any resources, e.g., ChatGPT, Co-pilot, is allowed
  - (still can't submit else's hw, obv)

# Recursion review

- Most recursion is structural (comes from data definitions)!

TEMPLATE

```
(define (lst-fn lst)
  (cond
    [(empty? lst) ...]
    [else ... (first lst) ... (lst-fn (rest lst)) ...]))
```

Data Def

```
;; A List<X> is
;; - empty
;; - (cons X List<X>)
```

# A Different Kind of Recursion!

- Not all recursion is structural (comes from data definitions)!

```
(define (lst-fn lst)
  (cond
    [(empty? lst) ...]
    [else ... (first lst) ... (lst-fn (rest lst)) ...]))
```

```
;; A List<X> is
;; - empty
;; - (cons X List<X>)
```

# A Different Kind of Recursion!

- Not all recursion is structural (comes from data definitions)!

```
;; gcd : Nat Nat -> Nat
;; computes greatest common divisor, using Euclid's algorithm
;; termination argument:
;; m is halved (at least) every step (modulo fn)
(define (gcd n m)
  (if (= m 0)
      n
      (gcd m (modulo n m))))
```

What template is this following??

# A Different Kind of Recursion!

- **Non-structural recursion** (doesn't come from data definitions) is called **generative recursion**
- no template, but requires **Termination Argument**
  - Explains why the function terminates!

```
;; gcd : Nat Nat -> Nat
;; computes greatest common divisor, using Euclid's algorithm
;; termination argument:
;; m is halved (at least) every iteration (by modulo fn)
(define (gcd n m)
  (if (= m 0)
      n
      (gcd m (modulo n m))))
```

Recursive call must be on "smaller" version of the problem